

Optimization of titanium cranial implant designs using generalized reduced gradient method, analysis of finite elements, and artificial neural networks

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Abstract

When cranial bone needs to be removed or lost, subsequent reconstruction of the defect is necessary to protect the underlying brain, correct aesthetic deformities, or both. Cranioplasty surgical procedures are performed to correct the skull defects requiring reconstruction of form and function. Personalized cranial implants can repair severe injuries to the skull can be done through This study presents the optimization of cranial titanium implants. A total of sixty different models were subjected to a simulation by Finite Element Analysis (FEA) applying the mechanical properties of a grade 5 titanium alloy (Ti6Al4V) implant material. The material was subjected to intracranial pressure (ICP) conditions, with a typical range (10 mm Hg) and twelve fixation points in the boundary conditions. An artificial neural network (ANN) was created to connect the designs, obtaining maximum displacements. Optimal designs were obtained using a generalized reduced gradient that minimizes the amount of material, maintaining as a restriction a maximum displacement of 0.1 mm for the 5th to 95th percentiles, which represent the group of individuals under study.

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1. Introduction

The human head is often subjected to impact during automobile accidents, falls, or sport-related events. These impact conditions can lead to mechanically induced head injury, which constitutes one of the major causes of accidental death [1]. Head injuries could be grouped into three categories: scalp damage, skull fracture, brain injury, or a combination of these [2,3].

Improving indications for cranial decompressive procedures, mainly after traumatic injuries and vascular lesions had led to a demand for effective bone substitutes in cranial reconstruction, particularly in large and complex bone defects. Cranioplasty is carried out to restore the morphological and functional anatomy of the cranial vault, to protect the brain, thus avoiding neurological disorders, deficits, or changes in the cerebrospinal fluid, and to restore cranial aesthetics [4,5]. Cranioplasty surgery does not only offer cosmetic and sometimes lifesaving benefits but also gives relief to psychological drawbacks and

improves the life quality for patients [6]. Cranioplasty surgical procedures may be conducted by using autografting (the implant is taken from the patient's body) and allografting (implant taken from a donor's body) or alloplastic (non-biologic such as polymeric and metallic) materials [7].

Metallic alloplastic materials, used in alloys with titanium, have mechanical properties greater than bone, manufacturing ease, and good resistance to corrosion degradation [8]. Besides, due to good mechanical properties superior to those of human bone, such as modulus of elasticity and yield strength, they lend themselves to load-bearing applications in the human body and prevent fractures after use.

Ti-containing alloys, such as the commonly used surgical Grade 5 titanium (Ti6Al4V), present low density, a high strength-to-weight ratio, high biocompatibility, and form an oxide layer to which bone progenitor cells can strongly adhere [9]. Titanium is used in the cranium for fixation devices such as plates and

screws, mesh, or solid plates, and in combination with other materials such as inert plastic or ceramic components [10].

The selection of cranial implants must satisfy several important criteria, such as biocompatibility, customized geometry to ensure direct contact with bone tissue, and sufficient mechanical properties to withstand function related stress [11]. Technical readiness for clinical application, short lead time, low cost, and ease of manufacture for alloplastic cranioplasty are also important considerations [12].

On the other hand, developments in tissue engineering are moving forward, exploiting advanced designs and fabrication technologies to design and produce implants, patterns or templates that enable the fabrication of custom-made prostheses without requiring a model of the anatomy to be made [13]. In this regard, the optimization of implants becomes relevant to reduce the weight, material usage, and cost of the implants while assuring their structural integrity and functionality [14], at the same time, parameters of the material such as porosity can be adjusted [15].

Particularly, the skull provides the structure to the head and face while protecting the brain, it is composed of flat and irregular bones. The skull can be divided into a facial part called Viscerocranium, the bones which form the face, and a Neurocranium, known as the braincase, that protects the brain and brainstem [16,17].

The presence of a lesion (intra- or extra-axial) can generate displacement of the brain's midline, causing herniation, compression of basal cisterns, increased intracranial pressure, and leading to death. A midline shift greater than 0.5 cm is a predictor of a bad result in the neurological outcome of patients with head injuries hospitalized in intensive care [18].

It is essential to classify the injury to address the diagnostic study of a seriously ill patient due to severe head trauma. The most widespread and defended of the classifications of traumatic brain injury (TBI) by CT is that of Marshall et al. [19], which is based on the state of the mesencephalic cisterns, the degree of deviation from the midline, and the presence or absence of focal lesion (Lesions diffuse-type I, II, III or IV).

Modern design and manufacturing engineering technologies have greatly improved how modern craniofacial implants are designed and fabricated. However, sophisticated optimization algorithms that simultaneously deal with multi-functional designs on multiple length scales need to be developed [14].

Artificial neural networks (ANN) models are successfully used in different fields of study; after they are satisfactorily competent and tested, it can generalize rules and respond rapidly (instantaneously) to input data to predict required outputs within the domains covered by the training examples. Moreover, it can handle many data sets, implicitly detect the complex nonlinear relationships between dependent and independent variables, and detect all possible interactions between predictor variables [20,21]. The multi-layer perceptron (MLP) network, typically referred to as back propagation (BP) network, is the most popular ANN in engineering issues and may have one or several hidden layers.

The optimization is to obtain the best possible result in a process or system by determining the values of the variables that intervene; in mathematical terms, it consists of searching for a minimum or maximum of a function. For example, the design of bone implants allows the design of structures to meet the desired objectives and restrictions [22,23]. The generalized reduced gradient or GRG search method is a nonlinear constraint optimization method used in the Excel Solver [24].

Implementing computer-aided design (CAD) and optimization in implant design is hampered by the high computational cost; however, the application of neural networks can solve the problem by reducing simulation times. In addition, the integration of optimization technology with simulation and artificial intelligence techniques will reduce experimental times and costs.

This study aims to determine the optimal design that minimizes the amount of Ti6Al4V material, subject to a maximum displacement constraint of 0.1 mm (total analysis deformation), for a neurocranial implant. The rest of the paper is organized in materials and methods, where it is presented from data acquisition, implant design, functional finite element analysis, and artificial neural network. Subsequently, a results section presents a normality test, implant design, functional analysis, predictive neural network, GRG optimization, and finally, the conclusions.

The challenge of this article is to determine the savings obtained by minimizing the volume of material and the cost savings by reducing the design time of the implant, concerning other methodologies recorded in specialized literature. To overcome it, a future investigation is recommended where the cost factor is measured.

2. Materials and methods

The proposed methodology for the design and optimization of titanium cranial implants is shown in the block diagram in Figure 1. The whole methodology is divided into five modules: data acquisition, implant design, finite element analysis (FEA), artificial neural network (ANN), and optimization (GRG method).

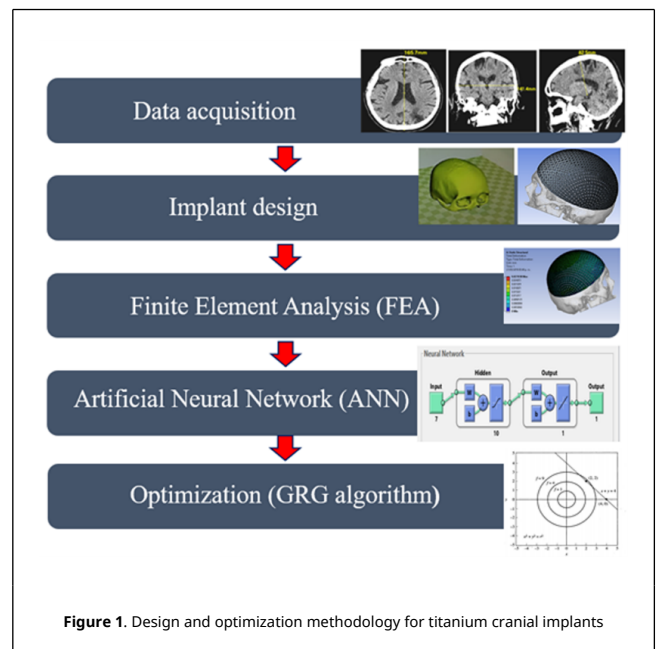


Figure 1. Design and optimization methodology for titanium cranial implants

2.1 Data acquisition (cranial anatomy approach)

In the present study, six variables were selected using anatomical points, and a craniometric study was performed (130 Mexican adult skulls with ages between 18 and 50 years were analyzed). The participants of the study come from fourteen different states (Chihuahua, Guerrero, Sinaloa, Sonora, Tijuana, Hidalgo, Jalisco, Mexico City, Guanajuato, Colima, Coahuila, Queretaro, and Veracruz). The inclusion criteria were free of physical injuries, without cranial fracture, deformities, or

surgeries in the skull.

An anthropometer brand Rosscraft model Campell® 10 RC-10 with 18 cm range, a Rosscraft metallic ribbon for anthropometric use with 200 cm range, each equipment has an accuracy of 0.5 mm; and an ErgoMeasure vertical anthropometer with 500 cm range and precision of ±1mm; were used to measure the anthropometric dimensions.

The anthropometric dimensions used in the study indicate the distance between two referenced craniometric points: Glabella (G), Vertex (V), Opisthocranium (Op), and Eurion (Eu). Figure 2 shows an overview of the skull bones of the Neurocranium (Frontal, Parietal, Temporal and Occipital bones) and the variables (craniometric dimensions) used in the study with craniometric reference landmarks: Eu-Eu = head width (1), G-Op = skull length (2), V-G = head height (3), Eu-V-Eu = Semicircular length of Eu-V-Eu (4), G-V-Op = Semicircular length G-V-Op (5) and head circumference (6).

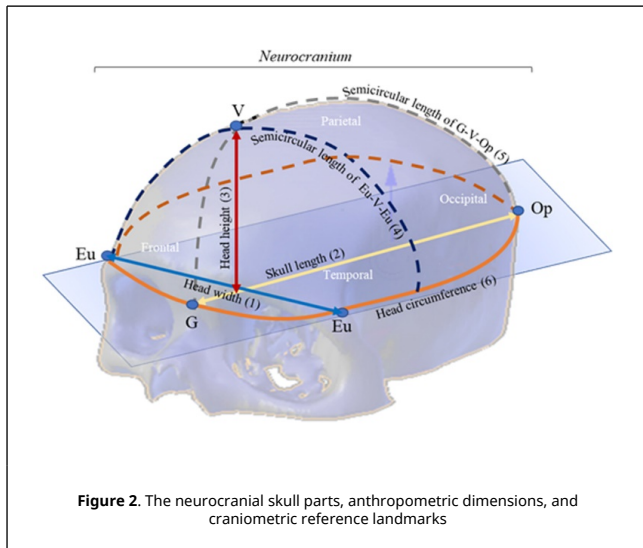


Figure 2. The neurocranial skull parts, anthropometric dimensions, and craniometric reference landmarks

Following the ethics committee of the Autonomous University of Ciudad Juárez (UACJ), the protocol applied was reviewed and approved. The participants signed a consent form accepting their participation in the study and the absence of health risks when participating in the study. The information collected was treated confidentially and was used only for academic purposes. A team of 3 anthropometrics was trained to perform cranial anthropometric measurements. Descriptive statistics (mean, standard deviation, minimum, maximum, range, and 5th, 25th, 50th, 75th, and 95th percentiles) were calculated. The Kolmogorov-Smirnov test was applied to ensure the normality of the data, considering a significance value of 0.05. All statistical procedures were conducted using SPSSv17 software.

2.2 Implant design

The design of the implant must satisfy two main requirements: geometry and functionality [25-27]. The functionality considers the geometry, dimensions, and materials to satisfy functional requirements such as structural performance. From the values obtained in the craniometric study, the values corresponding to the 5th, 25th, 50th, 75th, and 95th percentiles were selected. The bone implants were designed using SolidWorks software, applying the values obtained.

Different designs were performed for each percentile varying the thickness of the implant between 0.5 mm to 1 mm,

thickness commonly applied in commercial meshes, the size (diameter of 3 mm, 4 mm, 5 mm, and 6 mm), and separation of the holes (5° and 10°) in such a way that, for each percentile, there is a different geometry and volume. The percentage of empty spaces (A) was calculated using Eq.(1), where the total volume corresponds to the geometry without the holes and the final volume with holes. The volume values were determined using the software, while the models were exported in Parasolid format (*.x_t)

$$A = \left(\frac{\text{Total Volume} - \text{Final Volume}}{\text{Total Volume}} \right) (100) \quad (1)$$

The specifications of hole size, separation of holes and thickness of each design corresponding to 5th, 25th, 50th, 75th, and 95th percentiles are shown in Table 1.

Table 1. Implants design specifications

Specifications of design	1	2	3	4	5	6	7	8	9	10	11	12	Percentile
Hole diameter (mm)	3	3	3	3	4	4	4	4	5	5	6	6	5 th
Separation of holes (degrees)	5	5	10	10	5	5	10	10	10	10	10	10	
Thickness (mm)	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	
Specifications of design	13	14	15	16	17	18	19	20	21	22	23	24	Percentile
Hole diameter (mm)	3	3	3	3	4	4	4	4	5	5	6	6	25 th
Separation of holes (degrees)	5	5	10	10	5	5	10	10	10	10	10	10	
Thickness (mm)	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	
Specifications of design	25	26	27	28	29	30	31	32	33	34	35	36	Percentile
Hole diameter (mm)	3	3	3	3	4	4	4	4	5	5	6	6	50 th
Separation of holes (degrees)	5	5	10	10	5	5	10	10	10	10	10	10	
Thickness (mm)	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	
Specifications of design	37	38	39	40	41	42	43	44	45	46	47	48	Percentile
Hole diameter (mm)	3	3	3	3	4	4	4	4	5	5	6	6	75 th
Separation of holes (degrees)	5	5	10	10	5	5	10	10	10	10	10	10	
Thickness (mm)	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	
Specifications of design	49	50	51	52	53	54	55	56	57	58	59	60	Percentile
Hole diameter (mm)	3	3	3	3	4	4	4	4	5	5	6	6	95 th
Separation of holes (degrees)	5	5	10	10	5	5	10	10	10	10	10	10	
Thickness (mm)	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	0.5	1	

2.3 Normality test

Table 2 shows the normality test results, conducted using the Kolmogorov-Smirnov test. Due to the p-value of the six variables being higher than 0.05, data is considered normal, and it is possible to perform additional statistics and model analysis.

Table 2. Normality test results

Skull dimension	Kolmogorov Smirnov	P-value
Eu-Eu	0.462	0.983
G-Op	0.938	0.342
Head Circumference G-Op	0.650	0.791
G-V-Op	0.771	0.591
Eu-V-Eu	0.703	0.707
V-G	0.898	0.395

2.4 Data acquisition and implant design

Table 3 shows the descriptive statistics of craniometrics dimensions (mean, the standard deviation, the minimum, the maximum, and the 5th, 25th, 50th, 75th, and 95th percentiles) of head width (Eu-Eu), skull length (G-Op), head height (V-G), Eu-V-Eu Semicircular length, G-V-Op Semicircular length, and head circumference.

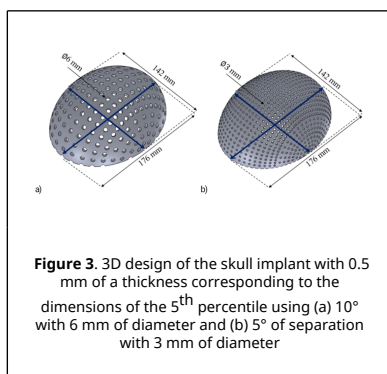
According to the percentiles values shown in Table 3, a total of sixty tridimensional implants were designed using SolidWorks software. Figure 3 shows two 3D designs of the skull implant, corresponding to the dimensions of the 5th percentile with variations in their geometry. The percentage of empty spaces (A) and the volume of each design are shown in Table 4.

Table 3. Craniometrics dimensions descriptive statistics

Descriptive statistics	Head width Eu-Eu (mm)	Cranial length G-Op (mm)	Head Circumference (mm)	G-V-Op Semicircular length (mm)	Head height V-G (mm)	Eu-V-Eu Semicircular length (mm)	
Mean ± SD	153.50 ± 6.71	190.40 ± 9.28	563.73±20.02	313.28 ± 29.50	76.57 ± 3.29	311.57 ± 19.51	
Minimum	138.70	171.00	508.00	261.00	69.70	263.30	
Maximum	170.00	218.70	614.00	525.00	86.60	370.00	
Percentiles	5	142.40	176.00	529.60	274.70	71.50	277.90
	25	148.60	183.70	551.30	297.70	74.20	297.90
	50	153.50	190.00	563.20	312.50	76.40	313.80
	75	157.80	195.70	577.70	325.80	78.50	325.00
	95	165.70	209.30	600.00	353.10	83.30	343.40

Table 4. Implant designs' percentage of empty spaces (A) and the volume

Specifications of design	1	2	3	4	5	6	7	8	9	10	11	12	Percent tile
Empty spaces (%)	17.1 2	18.3 8	4	5.21	31.8 8	33.2 1	7.17	8.41	11.3 5	12.6	16.6 2	17.8 8	5 th
Volume (mm ³)	151 04	299 68	175 21	348 07	126 20	250 00	169 18	335 95	161 42	320 43	151 93	301 45	
Specifications of design	13	14	15	16	17	18	19	20	21	22	23	24	Percent tile
Empty spaces (%)	15.8 8	15.9 7	3.71	3.73	29.5 2	29.6 8	6.66	6.69	10.5 4	10.6	15.4 2	15.5	25 th
Volume (mm ³)	168 13	333 74	192 29	382 07	143 30	284 08	186 26	370 04	178 50	354 48	169 61	335 51	
Specifications of design	25	26	27	28	29	30	31	32	33	34	35	36	Percent tile
Empty spaces (%)	20.7 3	16.7 3	9.98	11.5 3	24.2	18.2 2	12.4 3	12.8	15.0 9	14.1 1	18.0 1	15.4 9	50 th
Volume (mm ³)	181 78	360 96	205 95	409 30	156 95	311 29	199 91	397 23	192 15	381 70	182 66	362 73	
Specifications of design	37	38	39	40	41	42	43	44	45	46	47	48	Percent tile
Empty spaces (%)	18.5	15.7 2	8.39	10.6 8	21.7 5	17.1 7	10.7	11.9 1	13.2 1	13.1 9	15.9 5	15.0 3	75 th
Volume (mm ³)	195 16	385 88	204 65	434 22	169 44	336 20	212 41	422 15	218 45	406 62	194 28	387 64	
Specifications of design	49	50	51	52	53	54	55	56	57	58	59	60	Percent tile
Empty spaces (%)	15.1 1	3.51	3.53	27.8 9	28.0 4	6.31	6.34	9.98	10.0 3	14.5 9	14.6 7	14.5 2	95 th
Volume (mm ³)	220 92	439 02	245 18	487 46	196 04	389 24	239 09	475 36	231 32	459 81	221 81	440 79	



2.5 Functionality analysis (finite element analysis)

Sixty models were transferred to the ANSYS Workbench 18.1 (ANSYS Inc) to generate the FEA models. The FEA mesh of the computational model (Figure 4a) consisted of 10 nodes tetrahedral and 20 nodes hexahedral elements (Ansys non-linear elements). The minimum element size of the mesh was 0.5 mm for all models. Element sizes were chosen based on preliminary tests and sensitivity calculations. Subsequently, quality controls of the elements were carried out.

The use of titanium material (Ti6Al4V) was simulated. Table 5

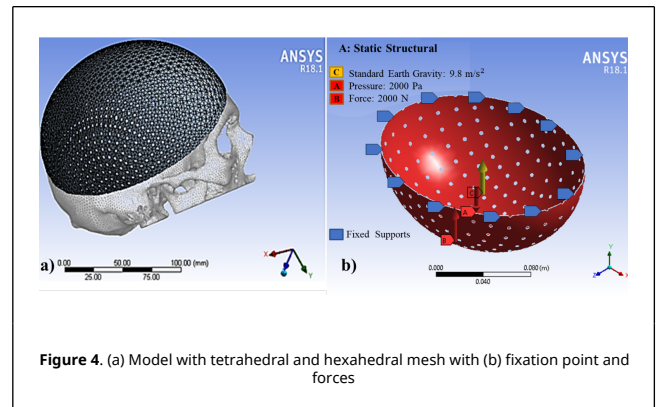
shows the mechanical properties of this material [28].

Table 5. Ti6Al4V Mechanical properties

Property	Value
Yield strength (σ_y)	896 MPa
Ultimate yield strength (σ_u)	965 MPa
Elastic modulus (E)	116 GPa
Poisson ratio	0.34

According to Nahum et al. [29] and Schneider et al. [30], minimum thresholds of 2450 N for men and 2000 N for women were suggested for clinically significant skull fractures. Messerer [31] determined that approximately 2000 N were needed to fracture the subcondylar region. In this study, a uniform distributed force of 2000 N was applied in the Y-axis in all the simulated designs located in the craniometric vertex (V), in the upper part of the implant, as seen in Figure 4b.

The static pressure of 10 mm Hg was considered based on intracranial pressure conditions [32] and a standard earth gravity of 9.8 m/s²; the pressure was applied on the inner surface and evenly distributed over an implant area. As Wen et al. [33], the bone-implant contact area was assumed to be complete osseous integration, and so the contact area was simulated by using a surface-to-surface option fully bonded. Both loading and boundary conditions of the FEA models are shown in Figure 4b.



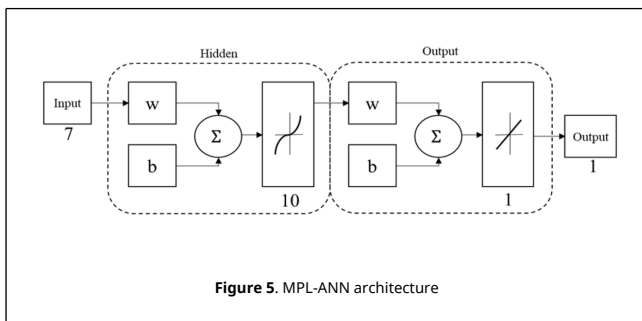
The screws to hold the implant are not simulated since these are considered independent elements of the implant. Although the screws interact with the model after surgery, their design is independent of the model proposed in this article; therefore, the structural integrity of the cranial implant is not affected during the design.

The mechanical properties of implants were all treated as isotropic, homogeneous, and linear elastic. Therefore, the safety factor is high in all the proposed designs, and large deformations are not considered since the element is expected to deflect (maximum displacement of 0.1 mm), but without exceeding the yield point, the element does not reach the plastic failure.

Because the present work focused on optimizing the geometry, the mechanical performance of the bone-implant construction was analyzed only in terms of the deformation parameter. According to Didier et al. [34], no study considers the phenomenon of "protection against stress" between the bone and the implant in its optimization process. Therefore, in this work, the optimization approach only considers the mechanical characteristics of the optimized part.

2.6 Artificial neural network application

An artificial neural network (ANN) based on multi-layer perceptron (MPL-ANN) was elaborated with the MATLAB Neural Network Toolbox to process the obtained data and create a predictive system that relates the anthropometric dimensions, the volume, and the thickness with the maximum displacement of the cranial implants designs. The MLP-ANN model predicted the maximum displacement. Figure 5 shows the final architecture of the MPL-ANN proposed. It consisted of three layers: an input, a hidden, and an output layer. Each layer consists of a few neurons and connections; weights were established between neurons. In the input layer, seven variables were introduced: thickness specifications, hole size, separation of holes, volume, head width, cranial length, and head height; the output layer was the maximum displacement of the designs. Randomly 70% of the data obtained in the simulation were used as training data, 15% as a validation, and the remaining 15% as a test. The performance and accuracy of the MLP model were examined by measuring the determination coefficient (R^2). Then, the values of the 30th, 40th, 60th and 80th percentiles were introduced to obtain the maximum displacement of their corresponding designs without submitting to simulation.



New theoretical designs were proposed for the 30th, 40th, 60th and 80th percentiles, which were not subjected to simulation; however, the maximum displacement was obtained for each of them using the artificial neural network created previously. This information was subsequently used for optimization.

2.7 Generalized reduced gradient optimization

The optimal point in a function corresponds to the value of x where the derivative $f'(x)$ is equal to zero. Furthermore, the second derivative $f''(x)$ indicates whether the optimum is a minimum or a maximum. If $f''(x) < 0$ (negative), it is a maximum; if $f''(x) > 0$ (positive), it is a minimum. In a two-dimensional function $f(x, y)$, the directional derivative $g'(0)$ can be calculated from the partial derivatives along the x and y axes, as shown Eq.(2), by:

$$g'(0) = f_x \cos\theta + f_y \sin\theta \quad (2)$$

where partial derivatives are evaluated at $x = a$ and $y = b$. The gradient (Eq.(3)) is a vector that is related to the directional derivative of $f(x, y)$ at the point $x = a$ and $y = b$

$$\nabla f(x, y) = \langle f_x(x, y), f_y(x, y) \rangle = f_x i + f_y j \quad (3)$$

The generalized gradient to n dimensions (Eq.(4)) is defined in vector notation as:

$$\nabla f(x) = \begin{bmatrix} f_{x_1}(x) \\ \vdots \\ f_{x_n}(x) \end{bmatrix} \quad (4)$$

Both the first and second derivatives offer valuable information in the search for the optimum. The first derivative provides a maximum tilt path for the function and indicates when the optimum has been reached. Once in the optimum, the second derivative $f''(x)$ will indicate if it is a maximum (negative) or if it is a minimum (positive). The determinant of a matrix formed with the second derivatives is known as the Hessian (H) of f :

$$H = \begin{bmatrix} f_{xx} & f_{yx} \\ f_{xy} & f_{yy} \end{bmatrix} \quad (5)$$

Equation (5) is the Hessian of f , in addition to providing a means of discriminating whether a multidimensional function has reached the optimum, allows searches that include second-order curvature. The GRG method requires the storage of an approximation of the Hessian matrix (Eq.(5)) and performs a search varying the displacement amplitude for the improvement of the reduced objective. The Excel solver is based on the GRG method, and they are evolutionary algorithms according to the input data and the objective function. First, a search direction is established to improve the objective function using a quasi-Newton procedure (BFGS), which requires the storage of an approximation of the Hessian matrix. Once the search direction is established, a one-dimensional search is performed using a variable step size procedure. The tool considers several points in the search space [35].

Using simple linear regression using the least squares method in Minitab statistical software, a multivariate linear regression model was obtained using four design variables (skull length, thickness, diameter, and hole spacing) as continuous predictors and final volume implant as a response variable as follows (Eq.(6)):

$$V = \beta_0 \pm \sum_{i=1}^n \beta_i X_i \pm \epsilon_i \quad (6)$$

where V is the response variable (Volume), X_i the independent variables or predictors, β_0 the intersection coefficient, β_i the linear coefficient, and ϵ_i the random experimental error.

Subsequently, using the Curve Fitting Toolbox of MATLAB, a polynomial function was found that best fits the data of the predictor variables length of the skull and the maximum displacement obtained by FEM with the final volume of the implant (response variable). The terms were identified as significant for selecting the models, and the highest adjusted R^2 value with a significance level of $p < 0.05$.

The optimal designs for each percentile that minimizes the Ti6Al4V material were found using a GRG method in an Excel solver, maintaining a maximum displacement of 0.1 mm as a restriction, since in this condition, a diffuse type II lesion may occur. The mesencephalic cisterns are present in diffuse-type II lesions, and the midline moderately deviates equal to or less than 5 mm [19]. The optimal designs were obtained by optimization equations where the minimum volume was used as the objective, using the maximum displacement (less than or equal to 0.1 mm) as the restriction. We optimized nine new theoretical designs for the 5th, 25th, 30th, 40th, 50th, 60th, 75th, 80th, and 95th percentiles and then validated them with MEF.

To solve the disadvantage of the generalized reduced gradient search method for finding the local minimum, the value of the step length was varied, and it was observed whether there was an improvement in the objective function. A search was performed with a different value if no improvement was observed. In the same way, the method can take us to a saddle point if the Hessian matrix is not positively defined. As all the identified eigenvalues of the Hessian matrix were positive, it can be determined that our function is being approximated by a quadratic function of circular or ellipsoidal contours that have a minimum.

3. Results

3.1 Functionality analysis and predictive neural network

The geometric models were subjected to the simulation by FEM in the ANSYS® software. Table 5 shows the results of the 60 simulations with an applied force of 2000N, where the displacements obtained corresponding to different designs are observed for the 5th, 25th, 50th, 75th, and 95th percentiles: at thicknesses of 0.5 and 1 mm. Figures 6 and 7 show the results of 10 of the 60 simulations; it could be noticed that displacements are greater for 0.5 mm than those established for 1 mm. The 75th percentile for 0.5 mm thickness shows the highest value, and the other percentiles observed are within the range of the maximum allowed offset. According to Figures 6 and 7, these displacements are observed mainly at the diametric base of each percentile studied.

Table 5. Implant designs' maximum displacement

Design	1	2	3	4	5	6	7	8	9	10	11	12	Percentile
Maximum displacement (mm)	0.161	0.034	0.105	0.011	0.117	0.027	0.084	0.008	0.086	0.017	0.092	0.027	5 th
Design	13	14	15	16	17	18	19	20	21	22	23	24	Percentile
Maximum displacement (mm)	0.154	0.034	0.071	0.113	0.054	0.030	0.066	0.137	0.073	0.187	0.087	0.24	25 th
Design	25	26	27	28	29	30	31	32	33	34	35	36	Percentile
Maximum displacement (mm)	0.211	0.038	0.060	0.113	0.057	0.029	0.063	0.137	0.073	0.151	0.03	0.23	50 th
Design	37	38	39	40	41	42	43	44	45	46	47	48	Percentile
Maximum displacement (mm)	0.207	0.039	0.061	0.113	0.034	0.019	0.065	0.12	0.095	0.20	0.39	0.46	75 th
Design	49	50	51	52	53	54	55	56	57	58	59	60	Percentile
Maximum displacement (mm)	0.183	0.035	0.075	0.111	0.092	0.006	0.070	0.15	0.080	0.017	0.092	0.19	95 th

mm). (d) 14 (percentile 50 with a thickness of 1 mm)

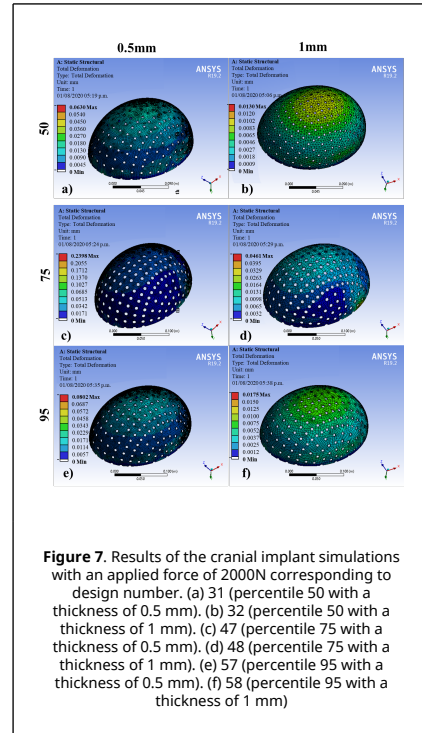


Figure 7. Results of the cranial implant simulations with an applied force of 2000N corresponding to design number. (a) 31 (percentile 50 with a thickness of 0.5 mm). (b) 32 (percentile 50 with a thickness of 1 mm). (c) 47 (percentile 75 with a thickness of 0.5 mm). (d) 48 (percentile 75 with a thickness of 1 mm). (e) 57 (percentile 95 with a thickness of 0.5 mm). (f) 58 (percentile 95 with a thickness of 1 mm)

To predict the mechanical behavior of the new designs (maximum displacements) of cranial implants, an MLP-ANN was elaborated to relate the created designs' specifications (thickness, hole size, separation of holes, volume, head width, cranial length, and head height).

Figure 8 shows the iteration in which the validation performance reached a minimum. The epoch is the number of times the algorithm was executed; in this case, the best validation performance was at epoch 4. As a result, the validation and test curves are remarkably similar; therefore, there is no excess of adjustment. Figure 9 shows the neural network selected based on its regression graph, where a global R² value of 0.9725 was obtained, showing a 97% relationship between the outputs of the network and the targets.

The ANN obtained was used to predict the maximum displacement of new theoretical designs of craniofacial implants for the 30th, 40th, 60th, and 80th percentile.

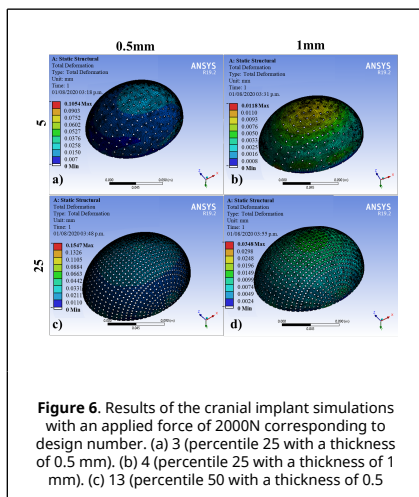


Figure 6. Results of the cranial implant simulations with an applied force of 2000N corresponding to design number. (a) 3 (percentile 25 with a thickness of 0.5 mm). (b) 4 (percentile 25 with a thickness of 1 mm). (c) 13 (percentile 50 with a thickness of 0.5 mm).

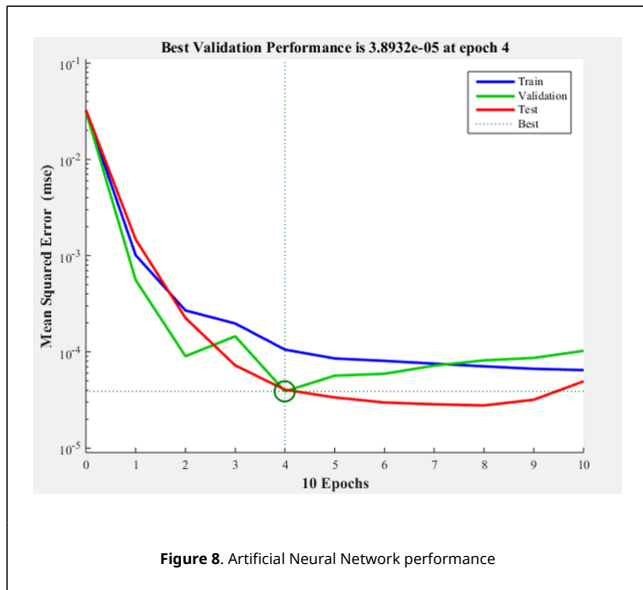


Figure 8. Artificial Neural Network performance

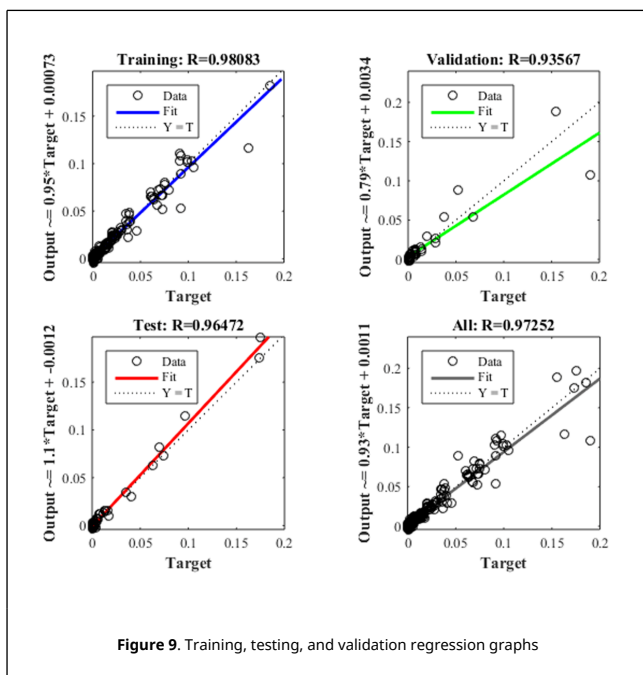


Figure 9. Training, testing, and validation regression graphs

3.2 Optimization

Using simple linear regression utilizing the Minitab statistical software, a linear model was obtained, applying the design variables as continuous predictors (skull length, thickness, diameter, and hole spacing) and the final implant volume as a response. The terms were identified as significant for selecting the model using the R^2 and general statistics of the significant F test. Table 6 shows the analysis of variance and the results of the R^2 DF (Degree of Freedom), SS Fit (Sum of Squares), MS Fit (Mean Square), the F value, and the P -value of the variables analyzed. The degrees of freedom indicate the number of independent elements in the sum of squares for each component of the model; having 60 different designs, we obtain a total of 59 DF, and the sum of squares (SS) is the deviation of the mean of the factor level estimated around the general mean. The Mean Square (MS) is an unbiased estimator of the variance and is the sum of squares divided by the degrees of

freedom. According to the values obtained in the F and P values, it was observed that each of the terms is statistically significant when obtaining p values < 0.05 and higher Fisher's F values with a significance level $\alpha = 0.05$. A mathematical model was developed to relate the design variables to the final volume of the implant, obtaining an R^2 of 0.97. Table 7 shows an adjusted R^2 of 97.31%, indicating that the model can estimate the volume using the design variables as predictors.

Table 6. Variance analysis

Source	DF	SS Adjust	MS Adjust	F-value	P-value
Regression	4	6211342822	1552835705	534.30	0.000
Skull Length (G-Op)	1	754802731	754802731	259.71	0.000
Thickness	1	5156845417	5156845417	1774.38	0.000
Diameter	1	100376598	100376598	34.54	0.000
Separation	1	292120699	292120699	100.51	0.000
Error	55	159845539	2906283		
Total	59	6371188360			

Table 7. Model summary

Standard error	R-square	R-squared (adjusted)	R-squared (predicted)
1704.78	97.49%	97.31%	96.94%

The relation between the variables skull length (x_1), thickness (x_2), diameter (x_3), and hole spacing (x_4) to the final implant volume (V) is presented in Eq.(7)

$$V = -62812 + 314.3(x_1) + 37083(x_2) - 1351(x_3) + 1043(x_4) \quad (7)$$

Using the anthropometric dimensions of the skull and modifying the design variables (thickness and percentage of empty spaces), a mathematical model was found in Matlab using the MATLAB Curve Fitting application (Figure 10), obtaining an R^2 of 0.97. Eq.(8) relates the length of the skull (x_1), the maximum displacement (y_1), and the volume (V) is as follows

$$V = -4.32x10^4 + 466.6(x_1) - 2.72x10^4(y_1) - 2336(x_1)(y_1) + 1.73x10^6(y_1)^2 \quad (8)$$

The resulting equations were entered as formulas in a spreadsheet in Excel. First, a cell was selected for each decision variable: the design variables thickness, diameter, and hole spacing. Then, a cell was created for the objective function, which corresponds to the final volume of the implant.

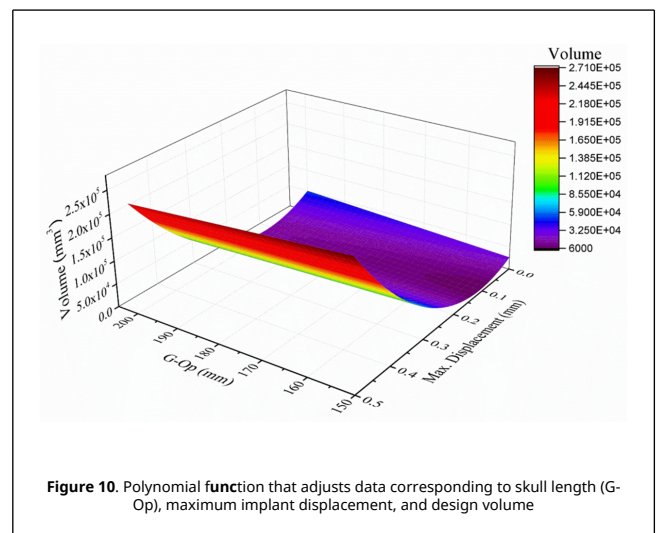


Figure 10. Polynomial function that adjusts data corresponding to skull length (G-Op), maximum implant displacement, and design volume

Finally, the optimal designs for each percentile were found using the solver tool, which minimizes the amount of material (Ti6Al4V) while maintaining a maximum displacement of 0.1 mm. The optimal designs are shown in Table 8 and were obtained with the minimum volume by Eq.(7) as the objective, using the maximum displacement of Eq.(8) as a restriction (minor or equal to 0.1 mm). The maximum displacement of these designs was validated using MEF and shown in Table 8.

Table 8. Values corresponding to the optimal designs of cranial implants

Percentile	x_1 Skull length (mm)	x_2 Thickness (mm)	x_3 Diameter (mm)	x_4 Separation (°)	V Volume (mm ³)	MEF Maximum displacement (mm)
5	176.00	0.56	4.77	5.18	12333.68	0.0843
25	183.70	0.55	4.80	5.15	14137.10	0.0906
30	185.00	0.55	4.81	5.15	14440.00	0.0934
40	188.00	0.54	4.75	5.19	15139.00	0.0969
50	190.00	0.53	4.76	5.18	15605.00	0.0991
60	193.18	0.52	4.70	5.24	16345.94	0.0997
75	195.70	0.52	4.71	5.23	16933.10	0.0989
80	196.00	0.52	4.72	5.23	17003.00	0.0974
95	209.30	0.50	4.74	5.20	18666.62	0.0912

4. Discussion

Nowadays, designing a 3D cranial implant model is a challenge. Some cranial implant models designed with Ti6Al4V and other polymeric materials have been proposed by other authors [36,37]. Morais et al. [38] proposed a Deep Learning (DL) approach toward automated CAD for the design of cranial implants. On the other hand, Stutz et al. [39] proposed machine learning-based approaches to shape completion. Wu et al. [40] proposed an architecture called 3D Shape Nets, in which the input shapes are given as input to a convolutional Deep Belief network that learns a probabilistic distribution from 3D volumes for 3D reconstruction. However, this type of network is difficult to train. For this study, the optimization of Ti6Al4V cranial implants was achieved by applying a novel proposal based on three tools, the generalized reduced gradient (GRG) search method, artificial neural networks (ANN), and applying the finite element method (FEM). According to work presented by Şensoy et al. [41], to optimize topologies for mandibular distractor plates and the geometry design, they used MATLAB-PYTHON-ANSYS and found superior stability with a less implant volume.

Ameen et al. [42] found an optimally designed implant with 0.5 mm thickness from test loading. In our case, optimal designs were found for the 5th to 95th percentiles, which minimizes the amount of Ti6Al4V material while maintaining a maximum offset of 0.1 mm, which is compatible with a large part of individuals of productive age of the Mexican population since they were considered in the data collection stage, individuals from 18 to 50 years of age, representative of 14 states of the Mexican Republic.

The optimization was based on the mechanical analysis (maximum displacement) of the design under the FEM simulation using normal intracranial pressure conditions (ICP = 10 mm Hg), twelve fixation points, and a force of 2000 N to lighten the structure (minimize volume) while maintaining the mechanical functionality and protection provided by the implant.

5. Conclusions

For this study, the optimization of Ti6Al4V cranial implants was achieved by applying a novel proposal based on three tools, the generalized reduced gradient (GRG) search method, artificial neural networks (ANN), and applying the finite element method (FEM). As a result, optimal designs were found for the 5th to 95th percentiles, which minimizes the amount of Ti6Al4V material

while maintaining a maximum offset of 0.1 mm, which is compatible with a large part of individuals of productive age of the Mexican population since they were considered in the data collection stage, individuals from 18 to 50 years of age, representative of 14 states of the Mexican Republic.

The optimization was based on the mechanical analysis (maximum displacement) of the design under the FEM simulation using normal intracranial pressure conditions (ICP = 10 mm Hg), twelve fixation points, and a force of 2000 N to lighten the structure (minimize volume) while maintaining the mechanical functionality and protection provided by the implant.

Using an ANN, it was possible to predict the response for numerous combinations of geometric parameters without creating or modifying new models by significantly reducing design and simulation time. The GRG optimization allowed us to identify the most efficient and lightweight conceptual designs, finding the geometries of the 3D models that require less volume of material for their manufacture, considerably reducing the final cost of the implant.

Future research proposes applying the same methodology and comparing different biocompatible materials; for example, in addition to Ti6Al4V, consider steel and polymethyl methacrylate, including the variable cost of the material. A second future investigation includes other software that facilitates the design stage, such as Easycrane, Easyimplant, MIMICS, Biobuild, MeVisLab, BioCAD, or 3D-Doctor. Also include other artificial intelligence tools such as simulated annealing metaheuristics, genetic algorithms, and taboo search to find the best solutions that reduce the volume of material and, consequently, the cost.

A third investigation that is proposed is to compare the monetary savings obtained by applying the methodology proposed in this work with other registered in specialized literature.

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