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Revisiting the Dissimilarity Representation in the Context of Regression

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ABSTRACT In machine learning, a natural way to represent an instance is by using a feature vector. However, several studies have shown that this representation may not accurately characterize an object. For classification problems, the dissimilarity paradigm has been proposed as an alternative to the standard feature-based approach. Encoding each object by pairwise dissimilarities has been demonstrated to improve the data quality because it mitigates some complexities such as class overlap, small disjuncts, and low-sample size. However, its suitability and performance when applied to regression problems have not been fully explored. This study redefines the dissimilarity representation for regression. To this end, we have carried out an extensive experimental evaluation on 34 datasets using two linear regression models. The results show that the dissimilarity approach decreases the error rates of both the traditional linear regression and the linear model with elastic net regularization, and it also reduces the complexity of most regression datasets.

INDEX TERMS Data complexity, Dissimilarity representation, Linear models, Regression

I. INTRODUCTION

N underlying step in machine learning and pattern recognition is the characterization of objects, where an ideal representation ensures building accurate learning algorithms [1]. Three approaches have emerged to represent a real-world object [2], [3]: the structural or syntactical approach using a symbolic data structure, the statistical approach based on a feature representation, and the class models.

The statistical approach assumes that an object is characterized by an *n*-dimensional vector $\mathbf{x} = [x_1, \ldots, x_n]^T \in \mathbb{R}^n$, where each x_i is a numeric attribute (feature) whose values are obtained through observation or as samples of the data (e.g., pixels of an image) [3], [4]. However, this representation may not capture the internal structure of some objects that have an intrinsic and detectable organization [5]–[7]. In classification problems, it is often difficult to obtain an appropriate feature-based characterization of objects, leading to a high-dimensional representation with class overlap or also a representation with a mixture of continuous and categorical features [5], [8].

Pękalska and Duin [9] proposed a dissimilarity representation in which objects are characterized by the difference or the dissimilarity to other objects from a representation set. A straightforward method of constructing the new representation is by means of mapping processes that convert a feature vector into a dissimilarity vector using a distance metric. Several studies have demonstrated that this alternative characterization suggests practical advantages over the feature representation, such as: i) it is possible to use a simple linear prediction model [10], ii) it yields a good separability between classes [11], iii) all dimensions in the dissimilarity space are equally relevant [11], and iv) the small disjunct problem is reduced [12].

Dissimilarity representation has been extensively applied to a variety of classification problems. For example, Bruno *et al.* [13] proposed a particular form of dissimilarity space for multimodal information, enabling fast and efficient interactive content-based retrieval of video data. Porro-Muñoz *et al.* [14] concluded that the use of the dissimilarity representation for the classification of chemical spectral data, which is characterized by changes in the shape of the spectra of different classes, outperformed the results achieved on the feature space.

Theodorakopoulos *et al.* [15] developed a method for pose-based human action recognition in the dissimilarity space. The problem of corporate bankruptcy prediction was tackled using four linear classifiers designed on the dissimilarity space, showing that their performance was considerably better than that of the models applied onto the feature space [10]. Orozco-Alzate *et al.* [1] investigated the suitability of a dynamic time warping based on the dissimilarity representation for distinguishing among the different seismic volcanic patterns. Classification of time series was carried out by using the dissimilarity representation [16].

Martins *et al.* [17] introduced a framework based on dissimilarity vectors and dynamic classifier selection to identify microscopic images of forest species. A two-stage model that consists of a feature selection algorithm and the dissimilaritybased representation for the classification of microarray gene expression data was proposed by García and Sánchez [18], who reported that the dissimilarity approach appears to be less sensitive to the number of genes than the feature-based representation. Also, the dissimilarity representation was combined with multiple classifier systems for text categorization [19].

To the best of our knowledge, far less research attention has been paid to the applicability of the dissimilarity representation to regression tasks. For instance, Jaramillo-Garzon *et al.* [20] modeled time-frequency representations by means of support vector regression, and the distance between regressions was calculated through dissimilarity measures based on dot products for the classification of phonocardiographic recordings. Silva-Mata *et al.* [21] combined the dissimilarity representation with the classical partial least square regression model for the recognition of substances and their chemical-physical properties in biochemical data. Despite these few works, we argue that the dissimilarity representation has not yet been deeply studied in the framework of regression problems.

This paper offers a large-scale experimental analysis with 34 benchmark regression datasets aiming to compare the performance of two linear models trained using feature and dissimilarity vectors. We intend to shed light on the suitability of the dissimilarity representation by addressing the following questions:

- 1) How the representation set size affects the predictive performance of regression models?
- 2) Does the dissimilarity representation reduce the complexity of a regression problem?
- 3) Do the dissimilarity-based linear regression models perform significantly better than the feature-based ones?

We cope with these issues by evaluating the dissimilarity representation constructed by means of the Euclidean distance and a random selection procedure designed to conform the representation set. To capture the difficulty of a regression problem, we compute a data complexity measure [22] to check whether or not the regression problem is simpler using the dissimilarity strategy than the traditional feature representation.

Henceforth the paper is organized as follows. Section II introduces the basis of the dissimilarity representation, whereas Section III describes the process for adapting the dissimilarity approach to regression problems. Next, Section IV provides the experimental set-up. In Section V, the results are presented and discussed. Finally, Section VI remarks the main conclusions and outlines possible future directions for extending this work.

II. THE DISSIMILARITY REPRESENTATION

The construction of the dissimilarity representation from the feature representation is based on measuring pairwise dissimilarities between an object and a set of prototypes or representative objects of each class $R = \{p_1, \ldots, p_M\}$. This R can be taken as the complete set of objects $T = \{\mathbf{x}_1, \ldots, \mathbf{x}_N\}$ or a subset of T ($R \subseteq T$), or even it can be defined as a set of generated prototypes [23]. The most straightforward method to select M prototypes from T is the random selection, which can be done either by ensuring that R contains prototypes of each class or by a global selection where R may not have examples from all classes. Several works have shown that an appropriate, intelligent selection strategy improves the performance owing to a better transformation of the feature space [24].

For the dissimilarity representation, we need a suitable dissimilarity measure $d(\cdot, \cdot)$ computed or derived from the objects; this dissimilarity measure must be non-negative $(d(\mathbf{x}_i, \mathbf{x}_j) > 0 \text{ if } \mathbf{x}_i \text{ is distinct from } \mathbf{x}_j)$ and obey the reflexivity condition $(d(\mathbf{x}_i, \mathbf{x}_i) = 0)$, but it might be non-metric. Common dissimilarity measures include Chi-square, Euclidean distance, Kolmogorov-Smirnov distance, cosine distance, Pearson correlation coefficient, Minkowski distance, and Spearman correlation.

A dissimilarity representation is defined as a datadependent mapping function $D(\cdot, R)$ from T to the dissimilarity space [9], [11]. This implies that each object $\mathbf{x}_i \in T$ can be represented by an M-dimensional realvalued vector in the dissimilarity space, $D(\mathbf{x}_i, R) =$ $[d(\mathbf{x}_i, p_1), \ldots, d(\mathbf{x}_i, p_M)]$, that is, each dimension corresponds to the dissimilarity computed between \mathbf{x}_i and a prototype $p_j \in R, (j = 1, \ldots, M)$. Then, the dissimilarities between all objects in T and the prototypes in R are represented by a matrix D(T, R) of size $N \times M$ [25]:

$$D(T,R) = \begin{bmatrix} d(\mathbf{x}_1, p_1) & d(\mathbf{x}_1, p_2) & \cdots & d(\mathbf{x}_1, p_M) \\ d(\mathbf{x}_2, p_1) & d(\mathbf{x}_2, p_2) & \cdots & d(\mathbf{x}_2, p_M) \\ \vdots & \vdots & \ddots & \vdots \\ d(\mathbf{x}_N, p_1) & d(\mathbf{x}_N, p_2) & \cdots & d(\mathbf{x}_N, p_M) \end{bmatrix}$$

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A representation space can now be built from this matrix. The dimensionality of the dissimilarity space is equal to M (the cardinality of R). Thus, each dimension corresponds to the dissimilarities with one of the prototypes in R. Note that the mapping process generates new variables to represent the data, thus changing the meaning of the original attributes.

III. DISSIMILARITY REPRESENTATION FOR REGRESSION

A regression problem involves a pair of measurements (\mathbf{x}, z) , where \mathbf{x} is called the independent variable and $z \in \mathbb{R}$ is the dependent variable. The aim of the regression is to find the function f(.) that can predict z from T based on Nobservations $(\mathbf{x}_i, z_i), i = 1, \ldots, N$.

Similar to the mapping process for converting a feature vector into a dissimilarity vector in classification tasks, in regression problems, the procedure is carried out for the learning and testing phases, as shown in the flowchart of Figure 1.



FIGURE 1. The mapping process into a dissimilarity representation. Dotted lines stand for the process to convert a test dataset into a dissimilarity dataset, whereas straight lines correspond to the step for building the dissimilarity regression training set.

The first step in constructing a dissimilarity matrix is to select an R from the training set. Here, this process is performed using a random selection method (Algorithm 1). Therefore, R was constructed by taking M random samples without replacement from T. In classification tasks, several instance selection methods have focused on extracting the most significant samples.

Algorithm 1: Random selection of the representation set Input: Regression training set $T = \{(\mathbf{x}_1, z_1), \dots, (\mathbf{x}_N, z_N)\},\$ K Number of samples to select. Output: Representation set $R \subseteq T$ /* Sampling without replacement */M = Generate K random numbers $\in [1, N]$ $R = \{\mathbf{x}_M\}$

The dissimilarity matrix is constructed using a dissimilarity measure once R has been selected, as shown in Algorithm 2; we used the Euclidean distance in the experiments. It should be noted that the resulting matrix D is a set that contains the target values taken from T. Remember that this mapping process should be performed in both the training and testing datasets. These dissimilarity sets are passed through the regression model for learning and predicting the independent variable of a new instance $\mathbf{x'}$.

Algorithm 2: Mapping process to construct a di	ssim-
ilarity matrix	

Input: Regression set $T = \{(\mathbf{x}_1, z_1), \dots, (\mathbf{x}_N, z_N)\},\$ Representation set $R = \{p_1, \dots, p_M\}.$ Output: Dissimilarity set D $D = \emptyset$ foreach $\mathbf{x}_i \in T$ do $\begin{bmatrix} distances = \emptyset \\ foreach p_j \in R \text{ do} \\ \\ distances = distances \cup \{dist_{i,j}\} \\ \\ D = D \cup \{distances\} \\ D = \{D, Z\} \end{bmatrix}$

The computational complexity of the proposed algorithm depends on the computational costs associated with the mapping process to construct a dissimilarity matrix D. For the training stage, both the time complexity and space complexity are $\mathcal{O}(N \cdot M)$, where N is the training set size and Mis the representation set size. As the testing stage uses R, the time and space complexities of mapping a test example are $\mathcal{O}(M)$.

IV. EXPERIMENTAL SET-UP

Considering that the ultimate goal of this work is to investigate the benefits of the dissimilarity representation over the feature representation in regression problems, we performed a systematic experimental study using two linear regression models that are tested over a pool of gold-standard datasets. In addition, a Wilcoxon's paired signed-rank test was employed to support the statistical validity of the results. The dissimilarity mapping process was implemented in the mlr3 library [26] and is available at https://github.com/JAIR-VG/ dissreg-tools.

A. DATASETS

Experiments were carried out on 34 benchmark small-and medium-sized regression datasets that are commonly used in some studies on regression [27]–[29]. Table 1 summarizes the main characteristics of these datasets, which were obtained from the following sources:

- 1) Torgo repository (https://www.dcc.fc.up.pt/~ltorgo/ Regression/DataSets.html)
- Weka dataset repository (https://waikato.github.io/ weka-wiki/datasets/)
- 3) Energy efficiency dataset used in [30]
- 4) Extrusion diameter dataset used in [31]
- 5) Residential building dataset used in [32]

For each dataset, the input variables were normalized in the range of [0, 1]. The quality estimation of the linear regression

models was generated using a 5-fold cross-validation. The resulting training and testing datasets were transformed by Euclidean distances using R.

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The training and testing processes of both regression models were carried out on the original dataset (feature representation) and the transformed dataset (dissimilarity representation). The performance results reported in this paper correspond to the averaged values from the five trials.

 TABLE 1. Overview of the databases (superscripts refer to the sources given in the list of database repositories and related articles).

No.	Dataset	Variables	Instances
1	Diabetes-numeric ¹	2	43
2	Quake ²	3	2178
3	Basketball ²	4	96
4	DeltaAilerons ¹	5	7129
5	MachineCPU ¹	6	209
6	DeltaElevators ¹	6	9517
7	Cooling ³	8	768
8	Heating ³	8	768
9	Bank-8FM ¹	8	8192
10	Kinematics ¹	8	8192
11	$Puma8NH^1$	8	8192
12	Calhousing ¹	8	20640
13	House8L ¹	8	22784
14	Stock ¹	9	950
15	PwLinear ²	10	200
16	2DPlanes ¹	10	40768
17	Friedman ¹	10	40768
18	CPUSmall ¹	12	8192
19	BodyFat ²	14	252
20	Pollution ²	15	60
21	ExtrusionOuter 4	15	260
22	ExtrusionInner ⁴	15	260
23	House16H ¹	16	22784
24	Elevators ¹	18	16599
25	CPUAct ¹	21	8192
26	Pyrimidines ¹	27	74
27	Wisconsin ¹	32	194
28	Bank32NH ¹	32	8192
29	Puma32H	32	8192
30	Ailerons ¹	40	13750
31	Pol ¹	48	15000
32	Triazines	60	186
33	SalesPrices ⁵	105	372
34	ConstructionCosts ⁵	105	372

B. REGRESSION MODELS

The two regression models evaluated in our experiments were the generalized linear model with elastic net regularization (GLM) and a linear regressor (LR). In a linear model, the response variable z_i is modeled by a linear function of explanatory variables x_j , j = 1, ..., n plus an error term ϵ_i (typically, it is assumed $\epsilon_i \sim N(0, \sigma^2)$) as follows:

$$z_i = \beta_0 + \beta_1 x_{1i} + \dots + \beta_n x_{ni} + \epsilon_i, \tag{1}$$

where β_j are the regression coefficients and x_{ji} are the regression variables.

In contrast with linear regression where the output is assumed to follow a Gaussian distribution, the generalized linear model [33] is a special class of nonlinear models where the response variable y_i does not need to be normally distributed, but it can follow some distribution from the exponential family (Poisson, multinomial, Bernoulli, chi-squared, gamma, and many others). Furthermore, homogeneity of variance does not need to be satisfied and errors need to be independent but not normally distributed.

A GLM is made up of a linear predictor $\eta_i = \beta_0 + \beta_1 x_{1i} + \cdots + \beta_n x_{ni}$, a smooth and invertible linearizing link function $g(\mu_i) = \eta_i$ that describes how the mean $(E(Y_i) = \mu_i)$ depends on the linear predictor, and a variance function $var(y_i) = \phi V(\mu_i)$ which describes the conditional distribution of the response variable y_i , that is, how the variance depends on the mean μ_i and a dispersion parameter ϕ .

The LR and the GLM with a Gaussian distribution were taken from the mlr3 framework [26] implemented in the R environment [34]. The default parameter values were used so that the results were not affected by a fine-tuning parameter step.

C. EVALUATION CRITERIA

We adopted two performance metrics commonly used in regression problems [29]. Both compute the numerical difference between the prediction of the model (\hat{z}_i) and the true value (z_i) [35]. First, the Root Mean Squared Error (RMSE) was defined as follows:

$$RMSE = \sqrt{\frac{1}{N_{test}} \sum_{i=1}^{N_{test}} (\hat{z}_i - z_i)^2},$$
 (2)

where N_{test} is the number of test samples.

The second metric was the Mean Absolute Error (MAE):

$$MAE = \sum_{i=1}^{N_{test}} | \hat{z}_i - z_i |.$$
 (3)

D. STATISTICAL TESTS

The Wilcoxon's paired signed-rank test was used to check for statistically significant differences between each pair of models. This statistic ranks the differences in the performances of the two algorithms for each dataset, ignoring the signs, and compares the ranks for the positive and the negative differences. Let d_i be the difference between the performance scores of the two models on *i*-th out of *L* datasets. Differences were ranked according to their absolute values. Let R^+ be the sum of ranks for the datasets on which the first model outperforms the second, and R^- the sum of ranks for the opposite. Ranks of $d_i = 0$ are split evenly among the sums; if there is an odd number of them, one is ignored:

$$R^{+} = \sum_{d_i>0} rank(d_i) + \frac{1}{2} \sum_{d_i=0} rank(d_i), \qquad (4)$$

$$R^{-} = \sum_{d_i < 0} rank(d_i) + \frac{1}{2} \sum_{d_i = 0} rank(d_i).$$
(5)

Let Z be the smaller of the sum, $Z = \min(R^+, R^-)$. If Z is less than or equal to the distribution value of Wilcoxon for L degrees of freedom, the null-hypothesis that both models perform equally well can be rejected.

E. DATA COMPLEXITY IN REGRESSION

Data complexity analysis was proposed in classification tasks as an approach to describing the intrinsic data characteristics [36]. The ultimate aim is to quantify some difficulties such as class ambiguity, boundary complexity, sample sparsity, and feature space dimensionality [36].

Lorena *et al.* [22] proposed several complexity measures to estimate the regression complexity. In this paper, we employed a feature correlation measure that captures the relationship between feature values and outputs. This is called the maximum feature correlation (C_1), where higher values indicate simpler problems, and lower values the opposite situation.

 C_1 takes the maximum correlation value over all feature dimensions and can be computed as follows:

$$C_{1} = \max_{j=1,\dots,n} |\rho(x_{j}, z)|,$$
(6)

where ρ is the Spearman correlation, x_j is the feature j, z is the independent variable, and n is the dimensionality.

V. RESULTS

The general objective of the experiments can be divided into a series of more specific purposes. First, we analyzed the effect of selecting different R sizes on the performance of the regression models. Second, we statistically checked whether or not the dissimilarity representation outperformed the feature representation when applied to regression. Finally, we compared the complexity of the dissimilarity-based datasets with that of the feature-based datasets.

A. INFLUENCE OF THE REPRESENTATION SET SIZE

In this experiment, we are interested in the impact of different R sizes over the dissimilarity regression models. We omitted the small-sized databases (Diabetes-numeric, Basketball, Pollution, Pyrimidines, and Triazines) and for the remaining 29 datasets, we randomly selected a number of representative objects ranging from 2 to 150. The upper bound was set to 150 because the random selection process cannot guarantee the optimal number of prototypes, whereas previous studies observed that selecting more than 150 objects did not produce significant differences [18].

When comparing and contrasting two or more datasets, it is important to represent them on comparable scales. Thus,



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FIGURE 2. Relative error difference for both regression models in terms of MRSE and MAE. Red and blue lines correspond to the average values across all datasets.

we defined a relative error difference [29], [37] computed for each dataset as follows:

$$Diff(D,F) = \frac{D-F}{F} \times 100, \tag{7}$$

where F and D represent the feature-based regressor and dissimilarity-based regressor results, respectively. Note that this score can be viewed as an indicator of improvement or deterioration of the dissimilarity-based model compared to the feature-based one.

Figure 2 shows the relative error difference of the 29 selected datasets achieved with the dissimilarity mapping process for all R sizes (2, ..., 150), where the red and blue lines correspond to the RMSE and MAE values averaged across all datasets, respectively. The x-axis represents the number of objects selected to construct R and the y-axis is the relative error difference in terms of RMSE (Figure 2–a, Figure 2–b) and MAE (Figure 2–c, Figure 2–d). Negative values indicate that the model using the dissimilarity representation was better than that based on the feature representation.

As can be observed from these plots, there appears a general tendency to reduce the error when increasing the R size. In addition, the relative error difference indicates that the regression models performed better when most datasets were transformed into a dissimilarity representation than with the original feature-based datasets. However, it was not possible to determine the optimal R size. Although the dissimilarity mapping process did not yield an error reduction when applied to some databases, we believe that the use of an intelligent prototype selection strategy instead of the random method could lead to the expected good behavior.

B. PERFORMANCE EVALUATION

Table 2 reports the RMSE and MAE values of both regression models, respectively. As the dissimilarity experiments were performed using different representation set sizes, for clarity and conciseness only the best RMSE and MAE values for each pair of dataset and regression model were collected. As can be observed, the best performances were mostly obtained by training the regressor with the dissimilarity-based datasets. In addition, for each performance measure, Table 3 summarizes how many times the regression models built on the dissimilarity representation were better/same/worse than the regressors based on the feature representation.

To determine whether or not the dissimilarity representation was better than the traditional approach, we ran a Wilcoxon's signed-rank test for detecting statistically significant differences using the results of RMSE and MAE. Table 4 shows the ranks and the *p*-values when comparing one representation against the other. Considering a significance level of $\alpha = 0.05$, the winner models are highlighted in bold when the associated *p*-value is lower than α . As can be seen, for all comparisons, the best algorithms were those trained with the data mapped into a dissimilarity space.

C. DATA COMPLEXITY IN DISSIMILARITY REGRESSION DATASETS

 C_1 was computed for each dataset in the feature representation as well as for the dissimilarity representation constructed from several R sizes. For the sake of simplicity and clarity, Table 5 summarizes the maximum C_1 values obtained from all dissimilarity datasets. The results show that, for some datasets, the mapping process converted a dataset into a simpler problem. However, this behavior was not observed in all the datasets, despite the fact that some of them achieved better results when using the dissimilarity representation.

VI. CONCLUSIONS AND FURTHER EXTENSIONS

A good object representation influences the performance of supervised machine learning methods. The dissimilarity representation has been used as an alternative to the feature characterization in classification problems, showing that dissimilarity-based classifiers may improve their accuracy. In addition, this mapping process presents important advantages regarding the reduction of some intrinsic data difficulties that allow the use of single linear models.

In this sense, the dissimilarity mapping process can also be used in the context of regression. Therefore, we performed an extensive experimental study on 34 benchmark regression datasets where each dataset was transformed into a dissimilarity matrix using the Euclidean distance and a set R. The independent variables in the new space correspond to the dissimilarity between the pairs of objects. From the experimental results, it is possible to draw some concluding remarks that support our findings:

- 1) Through a random selection of R of various sizes, it has been proven that mapping a feature sample into a dissimilarity space improves the performance of the linear regression models. On the other hand, it seems that in some cases, the use of a larger R can result beneficial.
- 2) The Wilcoxon's signed-rank test with $\alpha = 0.05$ validates our claim that the linear regression models built on the dissimilarity representation perform better than those based on the traditional feature-based representation.
- 3) Using a data complexity measure, it has been observed that the problems yield high correlation values when the datasets are mapped into a dissimilarity representation, that is, the problems become simpler.

The main criticism that can be made to the present work is the lack of a theoretical analysis. However, the experimental results have demonstrated the potential benefits of using the dissimilarity representation in the context of regression problems, thus opening some avenues for further research. One of them can be the design of systematic methods for the selection of representative objects specifically focused on regression tasks. Although it has been claimed that the Euclidean distance is suitable for dissimilarity transformation, other metrics should also be explored. In this sense,

TABLE 2.	Average RMSE a	and MAE values	(for each datas	set, the best resu	It is highlighted).
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		RM	ISE		MAE			
Datasets	GLM-F	GLM-D	LR-F	LR-D	GLM-F	GLM-D	LR-F	LR-D
Diabetes-numeric Quake Basketball DeltaAilerons MachineCPU	$\begin{array}{r} 6.6086e{-1} \\ 1.8935e{-1} \\ 9.1455e{-2} \\ 1.7484e{-4} \\ 8.8162e1 \end{array}$	$\begin{array}{c} 6.3962\mathrm{e}{-1} \\ 1.8935\mathrm{e}{-1} \\ 8.9383\mathrm{e}{-2} \\ 1.6834\mathrm{e}{-4} \\ 6.3543\mathrm{e}{1} \end{array}$	$\begin{array}{r} \hline 6.0247\mathrm{e}{-1} \\ 1.8887\mathrm{e}{-1} \\ 8.5302\mathrm{e}{-2} \\ 1.7195\mathrm{e}{-4} \\ 6.9117\mathrm{e}{1} \end{array}$	$\begin{array}{c} 6.4734\mathrm{e}{-1} \\ 1.8896\mathrm{e}{-1} \\ 8.5141\mathrm{e}{-2} \\ 1.6490\mathrm{e}{-4} \\ 5.4220\mathrm{e}{1} \end{array}$		5.044e-1 1.4927e-1 7.0860e-2 1.1898e-4 3.2306e1	$\begin{array}{r} \hline 4.7050e{-1} \\ \hline 1.4858e{-1} \\ \hline 6.7051e{-2} \\ \hline 1.2367e{-4} \\ \hline 4.1662e1 \end{array}$	$\begin{array}{c} 5.2263\mathrm{e}{-1} \\ 1.4837\mathrm{e}{-1} \\ 6.7526\mathrm{e}{-2} \\ 1.1570\mathrm{e}{-4} \\ 3.1331\mathrm{e}{1} \end{array}$
DeltaElevators Cooling Heating Bank-8FM Kinematics	$\begin{array}{r} \hline 1.4608e{-3} \\ 3.3464 \\ 3.0394 \\ 3.9509e{-2} \\ 2.0360e{-1} \end{array}$	$\begin{array}{c} 1.4340\mathrm{e}{-3} \\ 2.9734 \\ 2.6663 \\ 3.7539\mathrm{e}{-2} \\ 1.4339\mathrm{e}{-1} \end{array}$	$\begin{array}{r} \hline 1.4487e{-3} \\ 3.0857 \\ 2.8781 \\ 3.8820e{-2} \\ 2.0210e{-1} \end{array}$	$\begin{array}{c} 1.4252\mathrm{e}{-3} \\ 2.7977 \\ 2.4715 \\ 3.6591\mathrm{e}{-2} \\ 1.3837\mathrm{e}{-1} \end{array}$	$\begin{array}{r} \hline 1.1069e{-3} \\ 2.3760 \\ 2.1712 \\ 2.9357e{-2} \\ 1.6468e{-1} \end{array}$	$\begin{array}{c} 1.0859\mathrm{e}{-3}\\ 2.0835\\ 1.8259\\ 2.8804\mathrm{e}{-2}\\ 1.1028\mathrm{e}{-1}\end{array}$	$\begin{array}{r} \hline 1.1025e{-}3\\ 2.2980\\ 2.0802\\ 2.8556e{-}2\\ 1.6232e{-}1 \end{array}$	$\begin{array}{c} 1.0778\mathrm{e}{-3} \\ 1.9779 \\ 1.6839 \\ 2.8170\mathrm{e}{-2} \\ 1.0641\mathrm{e}{-1} \end{array}$
Puma8NH Calhousing House8L Stock PwLinear	4.4885 7.0222e4 4.2291e4 2.4112 2.3208	$\begin{array}{r} 3.9619 \\ 6.3125e4 \\ 3.4944e4 \\ 1.0329 \\ 1.8942 \end{array}$	$\begin{array}{r} 4.4639 \\ 6.9575e4 \\ 4.1544e4 \\ 2.3446 \\ 2.2064 \end{array}$	$\begin{array}{r} 3.8562 \\ 6.0647e4 \\ 3.3935e4 \\ 8.8450e{-1} \\ 1.7694 \end{array}$	$\begin{array}{r} 3.7287 \\ 5.1452e4 \\ 2.4536e4 \\ 1.8752 \\ 1.8519 \end{array}$	$\begin{array}{r} 3.2126 \\ 4.4760e4 \\ 1.9510e4 \\ 7.9780e{-1} \\ 1.5151 \end{array}$	$\begin{array}{r} 3.6460 \\ 5.0780e4 \\ 2.4349e4 \\ 1.8404 \\ 1.7525 \end{array}$	$\begin{array}{r} 3.1076 \\ 4.2730e4 \\ 1.8981e4 \\ 6.6056e{-1} \\ 1.4019 \end{array}$
2DPlanes Friedman CPUSmall BodyFat Pollution	2.3909 2.6432 1.0101e1 1.7145 4.0683e1	$\begin{array}{c} 1.1120 \\ 1.7696 \\ 3.6057 \\ 1.7270 \\ 4.0872e1 \end{array}$	2.3841 2.6310 9.8376 1.1956 4.7583e1	$\begin{array}{c} 1.0964 \\ 1.7277 \\ 3.3586 \\ 1.5080 \\ 3.7256e1 \end{array}$	$ \begin{array}{r} 1.9287 \\ 2.0674 \\ 6.0274 \\ 1.1216 \\ 3.0584e1 \end{array} $	$\begin{array}{c} 8.8403\mathrm{e}{-1} \\ 1.3683 \\ 2.6305 \\ 1.1992 \\ 3.1323\mathrm{e}{1} \end{array}$	$ \begin{array}{r} 1.9225 \\ 2.0384 \\ 6.1750 \\ 5.1532e-1 \\ 3.6088e1 \\ \end{array} $	$\begin{array}{r} 8.7236\mathrm{e}{-1} \\ 1.3399 \\ 2.3795 \\ 7.9893\mathrm{e}{-1} \\ 2.9796\mathrm{e}{1} \end{array}$
ExtrusionOuter ExutrusionInner House16H Elevators CPUActivity	$\begin{array}{r} \hline 1.2753e{-}2\\ \hline 1.0727e{-}3\\ 4.6408e4\\ \hline 2.9514e{-}3\\ 9.9122\\ \end{array}$	$\begin{array}{c} 1.2743\mathrm{e}{-2} \\ 1.0727\mathrm{e}{-3} \\ 4.0053\mathrm{e}{4} \\ 2.5907\mathrm{e}{-3} \\ 3.8733 \end{array}$	$\begin{array}{r} \hline 2.6372e-2\\ 1.3520e-3\\ 4.5481e4\\ 2.9058e-3\\ 9.6236\\ \end{array}$	$\begin{array}{c} 1.2993\mathrm{e}{-2} \\ 1.0748\mathrm{e}{-3} \\ 3.8915\mathrm{e}{4} \\ 2.4896\mathrm{e}{-3} \\ 3.5444 \end{array}$	$\begin{array}{c} \hline 3.8206e{-3} \\ 8.9223e{-4} \\ 2.5741e4 \\ 1.9875e{-3} \\ 5.8959 \end{array}$	$\begin{array}{c} 3.8206\mathrm{e}{-3} \\ 8.9223\mathrm{e}{-4} \\ 2.1860\mathrm{e}{4} \\ 1.8578\mathrm{e}{-3} \\ 2.6599 \end{array}$	$\begin{array}{r} \hline 8.0987e{-}3\\ 9.6523e{-}4\\ 2.5450e4\\ 1.9910e{-}3\\ 6.0697 \end{array}$	$\begin{array}{c} 4.1025\mathrm{e}{-3}\\ 8.9157\mathrm{e}{-4}\\ 2.1680\mathrm{e}{4}\\ 1.8330\mathrm{e}{-3}\\ 2.3484\end{array}$
Pyrimidines Wisconsin Bank32NH Puma32H Ailerons	$\begin{array}{r} \hline 1.3984e{-1} \\ 3.3216e1 \\ 8.4512e{-2} \\ 2.6948e{-2} \\ 1.7584e{-4} \end{array}$	$\begin{array}{c} 8.8503e{-}2\\ 3.2704e1\\ 8.6267e{-}2\\ 2.6884e{-}2\\ 1.6698e{-}4 \end{array}$	$\begin{array}{c} 2.2168e{-1} \\ 3.4254e1 \\ 8.3536e{-2} \\ 2.6763e{-2} \\ 1.7580e{-4} \end{array}$	7.7675e-2 3.1248e1 8.4312e-2 2.6707e-2 1.6373e-4	$\begin{array}{c} 9.6768e{-2} \\ 2.8484e1 \\ 5.8151e{-2} \\ 2.1253e{-2} \\ 1.2889e{-4} \end{array}$	$\begin{array}{c} 6.2905\mathrm{e}{-2} \\ 2.7799\mathrm{e}{1} \\ 6.0941\mathrm{e}{-2} \\ 2.1238\mathrm{e}{-2} \\ 1.2184\mathrm{e}{-4} \end{array}$	1.2751e-1 2.8487e1 5.8659e-2 2.0988e-2 1.2913e-4	$\begin{array}{c} 5.4419\mathrm{e}{-2} \\ 2.5426\mathrm{e}{1} \\ 6.0076\mathrm{e}{-2} \\ 2.0941\mathrm{e}{-2} \\ 1.1965\mathrm{e}{-4} \end{array}$
Pol Triazines SalesPrices ConstructionCosts	$\begin{array}{r} 3.0599e1 \\ 1.5312e{-1} \\ 1.7665e2 \\ 3.3477e1 \end{array}$	$\begin{array}{c} 1.3767e1 \\ 1.5009e{-1} \\ 4.6195e2 \\ 5.5326e1 \end{array}$	$\begin{array}{r} 3.0488e1 \\ 1.5689e{-1} \\ 1.7190e3 \\ 4.7211e2 \end{array}$	$\begin{array}{c} 1.2920 \mathrm{e1} \\ 1.4325 \mathrm{e-1} \\ 3.2565 \mathrm{e2} \\ 4.3560 \mathrm{e1} \end{array}$	$\begin{array}{r} \hline 2.6732 e1 \\ 1.1519 e-1 \\ 9.7319 e1 \\ 2.1410 e1 \end{array}$	$\begin{array}{c} 1.0229 \mathrm{e1} \\ 1.0921 \mathrm{e-1} \\ 3.1496 \mathrm{e2} \\ 3.3524 \mathrm{e1} \end{array}$	$\begin{array}{r} 2.6592 e1 \\ 1.1932 e-1 \\ 3.0033 e2 \\ 7.3097 e1 \end{array}$	$\begin{array}{r} 9.4926 \\ 1.0317\mathrm{e}{-1} \\ 2.2127\mathrm{e}{2} \\ 2.5363\mathrm{e}{1} \end{array}$

TABLE 3. Comparison of representation strategies. The three values in the cells show the number of datasets where the dissimilarity-based model of the row was better/same/worse than the feature-based regressor of the column.

		GLM-Feature	LR-Feature
RMSE	GLM-Dissimilarity LR-Dissimilarity	27/2/5	30/0/4
MAE	GLM-Dissimilarity LR-Dissimilarity	26/3/5	30/0/4

TABLE 4. Wilcoxon test for dissimilarity-based vs feature-based regressors.

	Comparison	R^+	R^{-}	<i>p</i> -value
RMSE	GLM-Dissimilarity vs GLM-Feature	494.5	100.5	4.4760e-4
	LR-Dissimilarity vs LR-Feature	551.0	44.0	1.7102e-6
MAE	GLM-Dissimilarity vs GLM-Feature	482.0	113.0	1.1152e-3
	LR-Dissimilarity vs LR-Feature	547.0	48.0	2.8280e-6

we believe that the adoption of distance metrics for highdimensional problems could be an interesting direction for extending the present work. Another point to investigate in the future can be to study the behavior of the dissimilarity representation for non-linear regression models, such as XG-Boost, K-nearest neighbors, support vector regressor and random forest. In addition, living in the Big Data era where data is growing exponentially, we would like to extend the present work by exploring the performance of the dissimilarity-based regression method on massive datasets, which bring a series of special computational challenges.

Finally, our proposal in its present form could not be applied to real-world applications in a continuous learning system, capable of incrementally storing and discarding streaming data. Thus the design of dissimilarity-based regression models with the power of continuous learning and adaptation during real-time operations under changes in the environment may constitute an interesting open line for further research.

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TABLE 5.	C1 values computed in the feature and dissimilarity
representa	tions.

Datasets	Feature	Dissimilarity
Diabetes-numeric	0.55	0.60
Ouake	0.05	0.06
Basketball	0.55	0.61
DeltaAilerons	0.80	0.75
MachineCPU	0.81	0.89
DeltaElevators	0.69	0.66
Cooling	0.86	0.91
Heating	0.86	0.93
Bank-8FM	0.70	0.18
Kinematics	0.52	0.50
Puma8NH	0.50	0.44
Calhousing	0.68	0.32
House8L	0.62	0.48
Stock	0.69	0.74
PwLinear	0.71	0.71
2DPlanes	0.69	0.61
Friedman	0.58	0.59
CPUSmall	0.73	0.76
BodyFat	0.99	0.79
Pollution	0.61	0.64
ExtrusionOuter	0.18	0.11
ExtrusionInner	0.10	0.12
House16H	0.60	0.43
Elevators	0.50	0.55
CPUAct	0.81	0.83
Pyrimidines	0.61	0.75
Wisconsin	0.33	0.35
Bank32NH	0.50	0.16
Puma32H	0.41	0.13
Ailerons	0.73	0.70
Pol	0.35	0.76
Triazines	0.28	0.31
SalesPrices	0.99	0.77
ConstructionCosts	0.97	0.88

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